



# Boundary Detection Using Actuated Sensor Networks

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[http://www.cens.ucla.edu/Project-Descriptions/Actuated\\_Boundary\\_Detection/index.html](http://www.cens.ucla.edu/Project-Descriptions/Actuated_Boundary_Detection/index.html)

## Introduction: Control law for Gradient descent

### Sensor-based Planning

- Generalized Voronoi Graphs (Choset et. al.) have been used to perform sensor-based navigation of robots (fig 1)
- Provably convergent in n-dimensions
- Control Law has been proposed for such gradient descent

$$\dot{x} = \alpha \text{Null}(\nabla G(x)) + \beta (\nabla G(x))^\dagger G(x)$$

where  $(\nabla G(x))^\dagger = (\nabla G(x))^T (\nabla G(x) (\nabla G(x))^T)^{-1}$

Alpha, beta → scalar gains

$G(x) = [d_1(x) - d_2(x)]$  and

$$\nabla G(x) = [(\nabla d_1(x) - \nabla d_2(x))^T]$$

### Adaptation to Sensor Networks

**Control law modified to suit randomly deployed sensor networks**  
 $G(x) = (\text{sensor reading at the mobile node}) - (\text{threshold reading defining the contour to be traced})$

and  $\nabla G(x) = (\nabla d_1(x) - \nabla d_2(x))$  where

$d_1 \rightarrow$  Unit vector in the direction of the steepest gradient **towards** the contour

$d_2 \rightarrow$  Unit vector in the direction of the steepest gradient **away** from the contour

Each iteration performs one query of sensor readings on all neighboring sensor nodes to compute  $d_1$  and  $d_2$  (Fig 2)

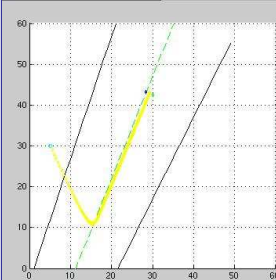


Fig 1 Robot traversing a Voronoi line using the control law

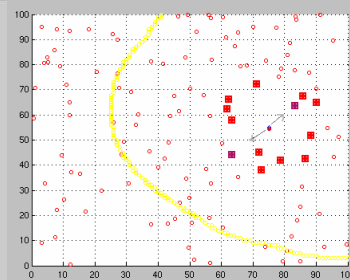


Fig 2 Gradient formation in the case of an actuated sensor node

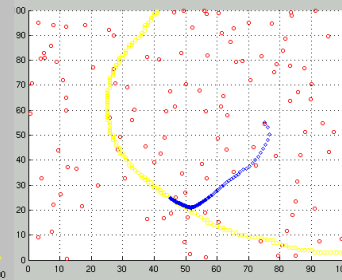
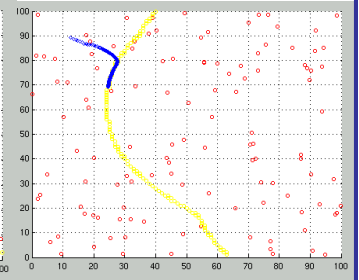


Fig 3,4: Two cases of Boundary Detection using Actuated sensor node and the adapted version of the control law



## Proposed Solution: Adapt control law to perform boundary detection using actuated nodes

### Assumptions

- Each node is perfectly localized
- The sensed phenomenon is assumed to monotonically degrade in a certain predefined fashion
- Algorithm not drastically affected by type of gradients

### Summary of results

- Algorithm uses only local sensor information
- **Saturation:** Boundary detection percentage is above 80% for networks of degree > 6
- **Optimality:** Traversed path is within 10-20% of optimal path for networks with degree > 6
- Algorithm minimally affected by type of degradation in the gradient

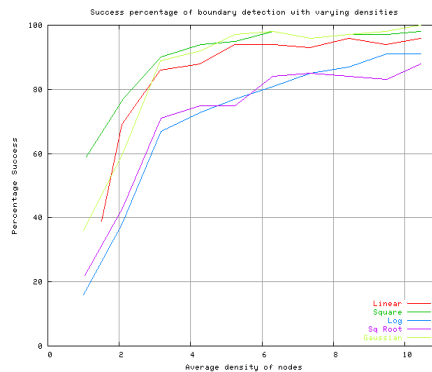


Fig 3: Percentage of success in detecting boundaries

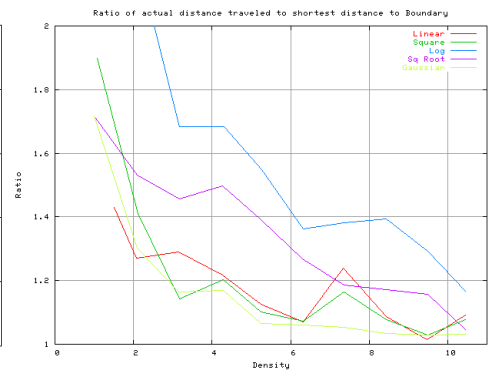


Fig 3: Optimality of path taken by the actuated sensor node